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Accounting Department Cracow University of Economics

BALANCE SHEET VALUATION OF SHARES BASED ON FAIR VALUE IN ACTIVE MARKETS ESTIMATED ON THE BASIS OF ECONOMIC AND FINANCIAL MODELS

Financial instruments pose a number of problems in economic sciences, especially in accountancy which deals with continuous measurements of these instruments in practice. One of the major problems is the use of fair value is valuating financial instruments. According to this category, two basic financial instruments ca be identified – instruments whose prices are determined by active markets and those for which such prices and markets do not exist. The first class is valuated on the basis of accounting categories while the second type of instruments is valuated on the basis of value estimation models and techniques. The paper presents the models for balance sheet valuation of shares based on fair value in active markets estimated on the basis of economic and financial models. The paper aims to present the results of empirical research and a comparison, on the basis of statistical methods, of valuations based on the actual fair value and estimated share values determined by economic and financial methods

Key words: accounting, financial instruments, fair value, balance sheet valuation, shares

Introduction. The major objective of the paper is to present the problems of the valuation of financial instruments in accounting. Most controversial issues relate to the category of fair value. This new accounting economic category, which is likely to become a general valuation principle, does not only refer to market transactions – as is commonly believed – but also to appropriate methods and expert opinions. In this context two basic types of financial instruments are defined – instruments with prices determined by active markets and those for which such prices and markets do not exist.

Because of a large number of primary and derivative instruments traded on the market, the paper focuses on the valuation of shares. The principles for balance sheet valuation based on fair value in active markets and estimations based on economic and financial models are identical for most financial instruments except those which are valuated on the basis of amortized costs (Bielawski, Wędzki 2002), (Bielawski 2005), (Bielawski, Wieliczko 2008).

The paper presents the concepts of share valuation based on general accounting principles, focusing on fair value in active markets and share value estimations based on economic and financial models. Balance sheet valuation of shares is based on selected models: DCF (*Discounted Cash Flow*), CAPM (*Capital Asset Pricing Model*) and HEV (*Historical Exchange Value*).

The last part of the paper refers to statistical methods to assess balance sheet valuations of listed shares representing two segments: 250 Plus companies (with capitalization exceeding EUR 250m) and 50 Plus (with capitalization ranging from EUR 50m to EUR 250m) from the point of view of their practical applications.

Balance sheet valuation of shares at fair value in active markets. The contemporary accounting standards accept two basis methods for valuating financial instruments: historical costs and fair value. Historical costs constitute a basis for valuations in all accounting standards, and the application of international standards

suggests that historical costs represent the most frequently applied method in preparing financial statements (International Financial Reporting Standards 2011). It implies that financial instruments are valuated on the basis of mixed models.

Mixed valuation models originate from the need to find an alternative valuation concept which could replace the fundamental principle of historical costs. Accounting theoreticians share the view that valuation should be based on historical costs and value (Wolk, Tearney 1997), (Bielawski, Garlińska-Bielawska 1999), (Riahi-Belkaoui 2000), (Surdykowska 2001), Hendriksen, Van Breda 2002). However, the problem is which concept of value should be chosen: fair value, market value, utility value, present value, economic value or another category of value? The choice is fair value.

The original reason for introducing fair value was to bring the measurement of economic categories in financial statements closer to the level of their actual value. This new economic category, a substitute of market value, does not only refer to the context of market transactions but also to valuations based on appropriate methods or techniques and expert opinions. According to this economic category, two basic types of shares are those traded in active markets and those for which prices and markets do not exist. The most reliable fair value is determined by an active market. However, when share valuation cannot rely on prices quoted by active markets (such prices do not exist), share valuation is based on fair value estimation with the use of different valuation methods and techniques.

Shares are originally recorded at fair value. This category ensures the stability of balance sheet items, while continuous adjustments of fair value and referring them directly to profits and losses hinder the current monitoring of revenues. Following the initial recording, shares continue to be recorded at fair value, and if they are held by a business entity until the time of preparing financial statements, they are evaluated at fair value at the date of the balance sheet. When changes in fair value are determined by active markets, this category does not pose any practical problems to the valuation process (Bielawski 2007), (Bielawski 2008), (Bielawski, Garlińska-Bielawska 2008).

Balance sheet valuations in the paper are based on the shares of medium (50 Plus) and large (250 Plus) listed companies, and they are classified as financial assets at fair value with changes in P/L Account. This classification implies that shares are recorded at fair value at the balance sheet date (at year-end), based on active market prices. Balance sheet valuations are presented in Table 1.

Table 1. Balance sheet valuations – 50 Plus and 250 Plus companies at fair value at year-end, active market prices (PLN)

| Doto | Gra- | Dofolio | Krusz- | Canak | Dobios | Bank | Żwice | Votu | Stalpro- | Świe- |
|------------|-------|---------|--------|--------|--------|----------|--------|--------|----------|--------|
| Date | jewo | Rafako | wica | Sariok | Dębica | Handlowy | Żywiec | Kęty | dukt | cie |
| 31.12.1998 | 4.18 | 6.90 | 7.20 | 24.10 | 52.00 | 43.80 | 420.00 | 33.10 | 10.20 | 8.60 |
| 31.12.1999 | 4.00 | 6.55 | 9.00 | 32.10 | 43.50 | 61.40 | 365.00 | 55.20 | 8.50 | 16.20 |
| 31.12.2000 | 5.70 | 6.85 | 8.30 | 33.00 | 34.00 | 61.50 | 208.00 | 44.00 | 14.60 | 22.00 |
| 31.12.2001 | 7.10 | 6.40 | 5.95 | 26.50 | 31.90 | 64.00 | 230.00 | 46.20 | 10.65 | 28.80 |
| 31.12.2002 | 6.90 | 4.37 | 5.20 | 29.50 | 48.00 | 74.50 | 390.00 | 50.80 | 13.00 | 36.90 |
| 31.12.2003 | 20.80 | 6.60 | 29.30 | 106.00 | 128.00 | 57.70 | 434.00 | 135.00 | 26.00 | 77.20 |
| 31.12.2004 | 25.00 | 13.00 | 35.00 | 141.00 | 98.50 | 64.10 | 452.00 | 131.00 | 78.50 | 58.00 |
| 31.12.2005 | 35.50 | 19.85 | 26.10 | 133.00 | 65.00 | 66.50 | 484.50 | 125.50 | 78.00 | 51.00 |
| 31.12.2006 | 56.00 | 39.25 | 75.40 | 205.00 | 77.40 | 86.80 | 490.00 | 200.00 | 540.00 | 104.00 |
| 31.12.2007 | 53.00 | 11.12 | 42.05 | 185.00 | 105.20 | 99.90 | 640.00 | 160.00 | 750.00 | 67.90 |

Source: author's calculations.

Estimation of balance sheet values – shares of 50 Plus companies based on economic and financial models. The estimation of values of shares issued by 50 Plus

companies is based on 3 economic and financial models: DCF (Brealey, Myers 1991), (Kolb, Rodriguez 1992), (Jajuga, Jajuga 1998), (Luenberger 2003), HEV (Otnes, Enochsen 1978), (Dobija 1995), and CAPM (Mossin 1966), (Sharpe 1964), (Lintner 1965).

Fair value estimations with the use of DCF, HEV and CAPM models are based on share prices recorded in the period of 10 years (1998-2007) on a monthly basis (for each company t = 120 observations). Fair value is estimated on the basis of 5 listed companies representing the 50 Plus segment: Grajewo, Rafako, Kruszwica, Sanok and Dębica. Balance sheet valuations at fair value based on economic and financial models are performed at the end of each analysed year (from 31.12.1998 to 31.12.2007). The estimations in this period are also based on the following indicators: WIG annual returns, WIG20 annual returns, average monthly increase in WIG returns, average monthly increase in WIG20 returns, annual inflation rates and annual risk-free returns.

The first model for estimating the fair value of listed shares is based on DCF. The model is used in 4 variants. The cash flow discounting factors are as follows: WIG annual returns, WIG20 annual returns, average monthly increase in WIG returns and average monthly returns in WIG20. The results of estimated balance sheet valuations based on DCF are presented in Tables 2-3.

Table 2. Estimated share values – 50 Plus companies, based on DCF according to WIG annual returns and WIG20 annual returns (PLN)

| Method | D | CF – W | IG annua | al returns | | DC | F – WIG | 20 annu | ıal returi | าร |
|------------|---------|--------|----------------|------------|--------|---------|---------|----------------|------------|--------|
| Date | Grajewo | Rafako | Krusz- wica | Sanok | Dębica | Grajewo | Rafako | Krusz- wica | Sanok | Dębica |
| 31.12.1998 | 17.53 | 8.68 | 10.78 | 46.45 | 75.36 | 16.54 | 8.19 | 10.17 | 43.84 | 71.13 |
| 31.12.1999 | 5.91 | 9.75 | 10.18 | 34.06 | 73.49 | 6.02 | 9.94 | 10.38 | 34.73 | 74.93 |
| 31.12.2000 | 3.95 | 6.46 | 8.88 | 31.68 | 42.93 | 4.06 | 6.65 | 9.14 | 32.60 | 44.17 |
| 31.12.2001 | 4.45 | 5.34 | 6.47 | 25.74 | 26.52 | 3.79 | 4.56 | 5.52 | 21.96 | 22.62 |
| 31.12.2002 | 7.33 | 6.60 | 6.14 | 27.35 | 32.92 | 6.91 | 6.23 | 5.79 | 25.78 | 31.04 |
| 31.12.2003 | 10.00 | 6.33 | 7.54 | 42.75 | 69.56 | 9.24 | 5.85 | 6.96 | 39.50 | 64.27 |
| 31.12.2004 | 26.61 | 8.44 | 37.49 | 135.61 | 163.76 | 25.91 | 8.22 | 36.50 | 132.03 | 159.43 |
| 31.12.2005 | 33.41 | 17.38 | 46.78 | 188.45 | 131.65 | 33.85 | 17.60 | 47.40 | 190.94 | 133.39 |
| 31.12.2006 | 50.27 | 28.11 | 36.96 | 188.33 | 92.04 | 43.93 | 24.56 | 32.30 | 164.59 | 80.44 |
| 31.12.2007 | 61.82 | 43.33 | 83.23 | 226.30 | 85.44 | 58.91 | 41.29 | 79.31 | 215.64 | 81.42 |

Source: author's calculations.

Table 3. Estimated share values – 50 Plus companies, DCF according to average monthly increase in WIG annual returns and average monthly increase in WIG20 annual returns (PLN)

| Method | DCF- | average WIG a | e month nnual re | • | ise in | DCF – average monthly increase in WIG20 annual returns | | | | | |
|------------|---------|------------------|---------------------|--------|--------|--|--------|----------------|--------|--------|--|
| Date | Grajewo | | Krusz- | | Dębica | Graje- wo | Rafako | Krusz- wica | Sanok | Dębica | |
| 31.12.1998 | 17.30 | 8.56 | 10.64 | 45.85 | 74.40 | 16.86 | 8.35 | 10.37 | 44.68 | 72.51 | |
| 31.12.1999 | 5.91 | 9.75 | 10.18 | 34.06 | 73.49 | 6.02 | 9.94 | 10.38 | 34.73 | 74.93 | |
| 31.12.2000 | 3.95 | 6.46 | 8.88 | 31.68 | 42.93 | 4.06 | 6.65 | 9.14 | 32.60 | 44.17 | |
| 31.12.2001 | 4.45 | 5.34 | 6.47 | 25.74 | 26.52 | 3.79 | 4.56 | 5.52 | 21.96 | 22.62 | |
| 31.12.2002 | 7.33 | 6.60 | 6.14 | 27.35 | 32.92 | 6.91 | 6.23 | 5.79 | 25.78 | 31.04 | |
| 31.12.2003 | 10.00 | 6.33 | 7.54 | 42.75 | 69.56 | 9.24 | 5.85 | 6.96 | 39.50 | 64.27 | |
| 31.12.2004 | 26.61 | 8.44 | 37.49 | 135.61 | 163.76 | 25.91 | 8.22 | 36.50 | 132.03 | 159.43 | |
| 31.12.2005 | 33.41 | 17.38 | 46.78 | 188.45 | 131.65 | 33.85 | 17.60 | 47.40 | 190.94 | 133.39 | |
| 31.12.2006 | 50.27 | 28.11 | 36.96 | 188.33 | 92.04 | 43.93 | 24.56 | 32.30 | 164.59 | 80.44 | |
| 31.12.2007 | 61.82 | 43.33 | 83.23 | 226.30 | 85.44 | 58.91 | 41.29 | 79.31 | 215.64 | 81.42 | |

Source: author's calculations.

The second method for estimating the fair value of shares is based on the CAPM model which expresses the expected return on shares as a sum of return on risk-free assets and a risk premium.

CAPM is applied in two variants. The first one assumes that the market rate of return is based on the WIG index, i.e. the entire market. The second variant of CAPM is based on WIG20 returns.

Considering the two above defined approaches to market returns and risk-free returns, CAPM is used to estimate expected returns and the value of listed shares at the end of each year (1998-2007). Risk-free returns are represented by annual interest rates of treasury bonds. The results of estimates based on CAPM for WIG and WIG20 indices are presented in the Table below.

Table 4. Estimated share values for 50 Plus companies based on CAPM for WIG and WIG20 annual returns (PLN)

| Method | | CAF | PM for W | /IG | | | CAPI | M for WI | G20 | |
|------------|---------|--------|----------------|--------|--------|---------|--------|----------------|--------|--------|
| Date | Grajewo | Rafako | Krusz- wica | Sanok | Dębica | Grajewo | Rafako | Krusz- wica | Sanok | Dębica |
| 31.12.1998 | 9.17 | 4.06 | 1 | 22.52 | 54.15 | 5.58 | 2.16 | I | 12.56 | 42.64 |
| 31.12.1999 | 7.95 | 13.51 | 17.75 | 46.76 | 88.46 | 8.48 | 14.45 | 19.31 | 49.97 | 93.40 |
| 31.12.2000 | 2.90 | 4.55 | 3.81 | 22.61 | 36.21 | 3.11 | 4.92 | 4.61 | 24.36 | 37.91 |
| 31.12.2001 | 1.12 | 0.88 | ı | 4.96 | 14.82 | - | ı | I | ı | 5.23 |
| 31.12.2002 | 6.78 | 6.05 | 5.14 | 25.12 | 31.46 | 5.56 | 4.87 | 3.40 | 20.36 | 27.37 |
| 31.12.2003 | 14.40 | 9.44 | 14.68 | 63.06 | 87.62 | 12.74 | 8.32 | 12.54 | 55.63 | 79.01 |
| 31.12.2004 | 33.77 | 10.98 | 59.22 | 175.02 | 189.76 | 32.56 | 10.57 | 56.30 | 168.54 | 184.19 |
| 31.12.2005 | 44.98 | 24.09 | 81.68 | 258.92 | 158.54 | 47.39 | 25.43 | 87.44 | 273.17 | 165.63 |
| 31.12.2006 | 71.64 | 41.45 | 70.81 | 274.80 | 115.13 | 56.28 | 32.24 | 51.48 | 214.41 | 94.11 |
| 31.12.2007 | 67.17 | 47.52 | 98.77 | 247.47 | 89.81 | 59.66 | 41.88 | 81.46 | 218.62 | 82.05 |

^{(-) -} Estimated balance sheet valuation based on the adopted method assumes negative values.

Source: author's calculations.

The last method for estimating the fair value of listed shares is based on the HEV model which considers an analysis of historical trends in actual share prices determined on the basis of exponential smoothing. Fair value estimations are based on two filtration factors: inflation rates and risk-free rate of return. Assuming that smoothing coefficient α is dependent on inflation rates and risk-free rates of return, balance sheet valuations of shares are performed for the analysed period (Table 5).

Table 5. Estimating share values, 50 Plus companies, based on HEV for annual inflation rates and annual risk-free returns (PLN)

| Method | HE | V – ann | ual infla | tion rate | S | HE | V – ann | ual risk- | -free retu | rns |
|------------|---------|---------|----------------|-----------|--------|-------------|---------|----------------|------------|--------|
| Date | Grajewo | Rafako | Krusz- wica | Sanok | Dębica | Grajew o | Rafako | Krusz- wica | Sanok | Dębica |
| 31.12.1998 | 17.49 | 9.42 | 11.49 | 48.42 | 80.62 | 16.19 | 9.18 | 11.07 | 46.05 | 77.82 |
| 31.12.1999 | 4.15 | 6.84 | 7.52 | 25.53 | 50.48 | 4.14 | 6.83 | 7.55 | 25.68 | 50.32 |
| 31.12.2000 | 4.27 | 6.60 | 8.89 | 32.24 | 42.01 | 4.44 | 6.63 | 8.82 | 32.33 | 41.02 |
| 31.12.2001 | 5.80 | 6.82 | 8.14 | 32.55 | 33.85 | 6.05 | 6.74 | 7.71 | 31.37 | 33.47 |
| 31.12.2002 | 7.10 | 6.37 | 5.94 | 26.55 | 32.16 | 7.07 | 6.10 | 5.84 | 26.95 | 34.29 |
| 31.12.2003 | 7.36 | 4.44 | 6.01 | 32.06 | 50.67 | 8.27 | 4.59 | 7.58 | 37.06 | 55.91 |
| 31.12.2004 | 21.15 | 7.14 | 29.78 | 108.95 | 125.51 | 21.31 | 7.38 | 29.99 | 110.27 | 124.40 |
| 31.12.2005 | 25.15 | 13.10 | 34.88 | 140.89 | 98.03 | 25.97 | 13.63 | 34.18 | 140.26 | 95.41 |
| 31.12.2006 | 36.07 | 20.39 | 27.46 | 134.99 | 65.34 | 37.11 | 21.38 | 29.98 | 138.67 | 65.98 |
| 31.12.2007 | 55.77 | 37.09 | 72.83 | 203.46 | 79.54 | 55.75 | 36.86 | 72.57 | 203.30 | 79.76 |

Source: author's calculations.

Estimating balance sheet share values, 250 Plus companies, based on economic and financial models. The estimations of the share values of large listed companies (250 Plus) are based on the same economic and financial models: DCF, CAPM and HEV. Calculations are based on quotations in the period of 10 years (1998 -2007) on a monthly basis (for each company t = 120 observations). Fair value is estimated for 5 listed companies: Bank Handlowy, Żywiec, Kęty, Stalprodukt and Świecie. Balance sheet valuations at fair value with the use of DCF, CAPM and HEV models are performed at year-end (31.12.1998 – 31.12.2007).

The first applied model for fair value estimations is DCF. The model is used in 4 variants. Cash flows are discounted in the following order: WIG annual returns, WIG20 annual returns, monthly average increase in WIG returns and monthly average increase in WIG20 returns. The results are presented in Tables 6-7.

Table 6. Estimating share values for 250 Plus companies based on DCF, WIG annual returns and WIG20 annual returns (PLN)

| Method | | DCF – V | VIG ann | ual returr | าร | | DCF - W | IG20 an | nual retui | rns |
|------------|-----------------------|---------|---------|------------------|---------|-----------------------|---------|---------|------------------|---------|
| Date | Bank Hand- Iowy | Żywiec | Kęty | Stal- produkt | Świecie | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie |
| 31.12.1998 | 44.25 | 303.21 | 42.94 | 20.16 | 15.77 | 41.77 | 286.19 | 40.53 | 19.02 | 14.89 |
| 31.12.1999 | 61.90 | 593.57 | 46.78 | 14.42 | 12.15 | 63.12 | 605.23 | 47.70 | 14.70 | 12.39 |
| 31.12.2000 | 60.60 | 360.24 | 54.48 | 8.39 | 15.99 | 62.35 | 370.63 | 56.05 | 8.63 | 16.45 |
| 31.12.2001 | 47.97 | 162.25 | 34.32 | 11.39 | 17.16 | 40.92 | 138.39 | 29.27 | 9.71 | 14.64 |
| 31.12.2002 | 66.04 | 237.34 | 47.68 | 10.99 | 29.72 | 62.27 | 223.78 | 44.95 | 10.36 | 28.02 |
| 31.12.2003 | 107.96 | 565.19 | 73.62 | 18.84 | 53.48 | 99.75 | 522.16 | 68.02 | 17.41 | 49.40 |
| 31.12.2004 | 73.82 | 555.24 | 172.71 | 33.26 | 98.77 | 71.87 | 540.58 | 168.15 | 32.38 | 96.16 |
| 31.12.2005 | 85.67 | 604.12 | 175.09 | 104.92 | 77.52 | 86.80 | 612.09 | 177.40 | 106.30 | 78.54 |
| 31.12.2006 | 94.17 | 686.07 | 177.71 | 110.45 | 72.22 | 82.29 | 599.57 | 155.31 | 96.52 | 63.11 |
| 31.12.2007 | 95.82 | 540.90 | 220.78 | 596.09 | 114.80 | 91.31 | 515.44 | 210.38 | 568.03 | 109.40 |

Source: author's calculations.

Table 7. Estimating share values for 250 Plus companies based on DCF, monthly average increase in WIG annual returns and monthly average increase in WIG20 annual returns (PLN)

| Method | DCF- | • | average nnual ret | increase urns | e in WIG | DCF – monthly average increase in WIG20 annual returns | | | | | |
|------------|-----------------------|--------|----------------------|------------------|----------|--|--------|--------|------------------|---------|--|
| Date | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie | |
| 31.12.1998 | 43.69 | 299.32 | 42.39 | 19.90 | 15.57 | 42.58 | 291.71 | 41.31 | 19.39 | 15.18 | |
| 31.12.1999 | 61.90 | 593.57 | 46.78 | 14.42 | 12.15 | 63.12 | 605.23 | 47.70 | 14.70 | 12.39 | |
| 31.12.2000 | 60.60 | 360.24 | 54.48 | 8.39 | 15.99 | 62.35 | 370.63 | 56.05 | 8.63 | 16.45 | |
| 31.12.2001 | 47.97 | 162.25 | 34.32 | 11.39 | 17.16 | 40.92 | 138.39 | 29.27 | 9.71 | 14.64 | |
| 31.12.2002 | 66.04 | 237.34 | 47.68 | 10.99 | 29.72 | 62.27 | 223.78 | 44.95 | 10.36 | 28.02 | |
| 31.12.2003 | 107.96 | 565.19 | 73.62 | 18.84 | 53.48 | 99.75 | 522.16 | 68.02 | 17.41 | 49.40 | |
| 31.12.2004 | 73.82 | 555.24 | 172.71 | 33.26 | 98.77 | 71.87 | 540.58 | 168.15 | 32.38 | 96.16 | |
| 31.12.2005 | 85.67 | 604.12 | 175.09 | 104.92 | 77.52 | 86.80 | 612.09 | 177.40 | 106.30 | 78.54 | |
| 31.12.2006 | 94.17 | 686.07 | 177.71 | 110.45 | 72.22 | 82.29 | 599.57 | 155.31 | 96.52 | 63.11 | |
| 31.12.2007 | 95.82 | 540.90 | 220.78 | 596.09 | 114.80 | 91.31 | 515.44 | 210.38 | 568.03 | 109.40 | |

Source: author's calculations.

The second method for fair value estimations is based on CAPM. The model is used in two variants. The first one assumes that the market rate of return is based on WIG, i.e. the entire market, while the other variant of CAPM is based on WIG20 returns.

Considering the two above defined approaches to market returns and risk-free returns, CAPM is used to estimate expected returns and the value of listed shares at the end of each year (1998-2007). The results of estimates based on CAPM for WIG and WIG20 indices are presented in the Table below.

Table 8. Estimating share values for 250 Plus companies based on CAPM, WIG annual returns and WIG20 annual returns (PLN)

| Method | | CAPM – | WIG ani | nual retur | ns | C | 4 <i>РМ -</i> И | /IG20 ar | nnual retu | ırns |
|------------|-----------------------|--------|---------|------------------|---------|-----------------------|-----------------|----------|------------------|---------|
| Date | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie |
| 31.12.1998 | 45.31 | 314.03 | 30.17 | 1 | 11.57 | 42.11 | 293.09 | 23.43 | 1 | 9.22 |
| 31.12.1999 | 60.83 | 578.24 | 56.85 | 28.69 | 14.50 | 62.80 | 596.25 | 60.08 | 31.47 | 15.29 |
| 31.12.2000 | 61.40 | 367.38 | 45.47 | 2.01 | 13.62 | 62.53 | 373.80 | 47.68 | 2.96 | 14.23 |
| 31.12.2001 | 49.77 | 171.33 | 18.32 | 1 | 9.99 | 41.56 | 144.79 | 5.56 | - | 3.94 |
| 31.12.2002 | 66.29 | 238.68 | 45.44 | 8.62 | 28.47 | 62.42 | 225.37 | 39.36 | 4.69 | 24.88 |
| 31.12.2003 | 105.59 | 546.58 | 93.82 | 42.61 | 66.62 | 99.28 | 514.95 | 84.45 | 35.89 | 60.17 |
| 31.12.2004 | 72.83 | 544.06 | 201.69 | 58.93 | 113.62 | 71.64 | 535.52 | 195.65 | 55.67 | 110.34 |
| 31.12.2005 | 84.19 | 588.47 | 212.89 | 209.08 | 92.52 | 86.37 | 603.17 | 222.58 | 225.34 | 96.58 |
| 31.12.2006 | 92.17 | 664.24 | 224.83 | 24510 | 89.37 | 82.01 | 593.43 | 183.11 | 172.51 | 73.30 |
| 31.12.2007 | 95.40 | 537.39 | 232.70 | 744.19 | 120.36 | 91.29 | 515.20 | 212.10 | 588.41 | 110.20 |

^{(–) –} Estimated balance sheet valuation based on the adopted method assumes negative values.

Source: author's calculations.

The third concept for fair value estimations is based on HEV. Fair value estimations are based on two exponential smoothing factors: inflation rates and risk-free returns. Assuming that smoothing coefficient α is dependent on inflation rates and risk-free rates of return, balance sheet valuations of shares are performed for the analysed period (Table 9).

Table 9. Estimating share values for 250 Plus companies based on HEV according to inflation rates and risk-free rates of return (PLN)

| to mination i | o milation rates and not not rates of retain (1 214) | | | | | | | | | |
|---------------|--|--------|-----------------------------|------------------|---------|-----------------------|--------|-------------|------------------|---------|
| Method | | HEV | inflation | on rates | | | HEV- | - risk-free | e returns | |
| Date | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie | Bank Hand- lowy | Żywiec | Kęty | Stal- produkt | Świecie |
| 31.12.1998 | 49.44 | 357.72 | 46.48 | 20.97 | 16.51 | 48.89 | 363.80 | 45.18 | 19.92 | 15.74 |
| 31.12.1999 | 46.94 | 410.18 | 37.04 | 9.90 | 9.96 | 47.27 | 409.16 | 37.46 | 9.86 | 10.10 |
| 31.12.2000 | 61.42 | 340.40 | 53.45 | 9.46 | 17.11 | 61.43 | 324.04 | 52.28 | 10.09 | 17.71 |
| 31.12.2001 | 61.67 | 209.53 | 44.15 | 14.33 | 22.47 | 62.13 | 213.51 | 44.55 | 13.61 | 23.70 |
| 31.12.2002 | 64.17 | 232.54 | 46.27 | 10.69 | 28.93 | 65.56 | 253.79 | 46.88 | 11.00 | 30.00 |
| 31.12.2003 | 73.94 | 391.47 | 53.61 | 13.43 | 38.25 | 72.84 | 394.35 | 59.12 | 14.29 | 40.88 |
| 31.12.2004 | 58.24 | 435.52 | 134.66 | 30.43 | 75.58 | 58.48 | 436.19 | 134.51 | 32.40 | 74.86 |
| 31.12.2005 | 64.13 | 452.45 | 130.92 | 78.49 | 57.90 | 64.32 | 454.99 | 130.49 | 78.45 | 57.35 |
| 31.12.2006 | 67.06 | 484.65 | 127.56 | 90.76 | 52.46 | 68.10 | 484.93 | 131.37 | 114.39 | 55.17 |
| 31.12.2007 | 87.81 | 501.54 | 196.92 | 556.15 | 101.22 | 87.91 | 502.73 | 196.61 | 557.82 | 100.94 |

Source: author's calculations.

An assessment of economic and financial models applied in estimating balance sheet share valuations based on statistical methods. The results of the study provide many valuable insights into the application of economic and financial models in estimating balance sheet values of shares issued by large and medium companies in the period of ten years in the context of comparability and reliability of financial statements. Assessments are based on DCF, HEV and CAPM models. The estimated balance sheet share valuations are referred to the actual fair value in active markets, which facilitates assessment based on statistical methods with the use of two statistical measures: maximum error and mean error (Aczel 2000).

The first assessment method is based on comparing the mean errors of balance sheet valuations performed with the use of the employed economic and financial models. The assessments of estimated balance sheet valuations for 250 Plus and 50 Plus companies are presented in Tables 10 and 12.

The second method is based on the maximum error – the recorded value between share value estimations for 250 Plus and 50 Plus companies and the actual fair value. Assessments based on the maximum value in the analysed period are presented in Tables 11 and 13.

Table 10. Assessment of models for estimating balance sheet share valuations for

250 Plus companies – mean error (%)

| Model | Bank Handlowy | Żywiec | Kęty | Stalprodukt | Świecie | Mean error (all companies) |
|---|------------------|--------|------|-------------|---------|-------------------------------|
| DCF – WIG annual returns | 9.95 | 14.17 | 5.92 | 3.46 | 10.13 | 8.73 |
| DCF – WIG20 annual returns | 4.88 | 9.88 | 1.73 | 7.24 | 5.67 | 5.88 |
| DCF – average monthly increase in WIG returns | 9.82 | 14.08 | 5.75 | 3.71 | 9.90 | 8.65 |
| DCF – average monthly increase in WIG20 returns | 5.06 | 10.01 | 1.97 | 6.88 | 6.01 | 5.99 |
| CAPM – WIG annual returns | 9.40 | 13.28 | 7.75 | 12.58 | 12.46 | 11.09 |
| CAPM – WIG20 annual returns | 4.84 | 9.68 | 0.92 | 35.83 | 3.78 | 11.01 |
| HEV – annual inflation rates | 4.77 | 3.09 | 5.06 | 11.44 | 1.94 | 5.26 |
| HEV – annual risk-free returns | 4.58 | 2.88 | 4.91 | 11.48 | 1.43 | 5.06 |

Source: author's research.

Table 11. Assessment of models for estimating balance sheet share valuations for 250 Plus companies – maximum error (%)

| Model | Bank Handlowy | Żywiec | Kęty | Stalprodukt | Świecie | Maximum error (all companies) |
|---|------------------|--------|-------|-------------|---------|-------------------------------|
| DCF – WIG annual returns | 87.11 | 73.19 | 45.47 | 97.60 | 83.42 | 97.60 |
| DCF – WIG20 annual returns | 72.87 | 78.19 | 49.62 | 86.51 | 73.12 | 86.51 |
| DCF – average monthly increase in WIG returns | 87.11 | 73.19 | 45.47 | 95.07 | 81.06 | 95.07 |
| DCF – average monthly increase in WIG20 returns | 72.87 | 78.19 | 49.62 | 90.11 | 76.46 | 90.11 |
| CAPM – WIG annual returns | 83.00 | 76.63 | 69.63 | 237.49 | 95.89 | 237.49 |
| CAPM – WIG20 annual returns | 72.05 | 79.71 | 87.97 | 333.64 | 90.24 | 333.64 |
| HEV – annual inflation rates | 28.14 | 63.65 | 60.29 | 105.62 | 91.99 | 105.62 |
| HEV – annual risk-free returns | 26.24 | 55.79 | 56.20 | 95.31 | 83.01 | 95.31 |

Source: author's research.

Table 12. Assessment of models for estimating balance sheet share valuations for 50 Plus companies – mean error (%)

| | 1 / | | | | | |
|---|---------|--------|----------------|-------|--------|----------------------------|
| Model | Grajewo | Rafako | Krusz- wica | Sanok | Dębica | Mean error (all companies) |
| DCF – WIG annual returns | 26.01 | 31.33 | 15.57 | 7.71 | 21.51 | 20.43 |
| DCF – WIG20 annual returns | 20.41 | 25.57 | 11.19 | 3.04 | 17.31 | 15.51 |
| DCF – average monthly increase in WIG returns | 25.47 | 31.17 | 15.38 | 7.46 | 21.33 | 20.16 |
| DCF – average monthly increase in WIG20 returns | 21.18 | 25.80 | 11.46 | 3.39 | 17.58 | 15.88 |
| CAPM – WIG annual returns | 16.86 | 36.56 | 13.24 | 5.76 | 26.52 | 19.79 |
| CAPM – WIG20 annual returns | 0.42 | 19.98 | 7.70 | 7.99 | 18.47 | 10.91 |
| HEV – annual inflation rates | 14.21 | 16.32 | 5.01 | 1.98 | 4.56 | 8.42 |
| HEV – annual risk-free return | 12.63 | 15.99 | 4.07 | 2.51 | 4.02 | 7.84 |

Source: author's research.

Table 13. Assessment of models for estimating balance sheet share valuations for 50 Plus companies – maximum error (%)

| · | . , | | | | | |
|---|---------|--------|----------------|--------|--------|-------------------------------|
| Model | Grajewo | Rafako | Krusz- wica | Sanok | Dębica | Maximun error (all companies) |
| DCF – WIG annual returns | 319.29 | 289.63 | 97.94 | 92.72 | 102.54 | 319.29 |
| DCF – WIG20 annual returns | 295.76 | 271.29 | 88.62 | 81.90 | 105.21 | 295.76 |
| DCF – average monthly increase in WIG returns | 313.91 | 289.63 | 97.94 | 90.25 | 102.54 | 313.91 |
| DCF – average monthly increase in WIG20 returns | 303.40 | 271.29 | 88.62 | 85.41 | 105.21 | 303.40 |
| CAPM – WIG annual returns | 119.31 | 327.32 | 212.93 | 94.67 | 143.91 | 327.32 |
| CAPM – WIG20 annual returns | 114.51 | 276.58 | 256.62 | 130.64 | 154.82 | 276.58 |
| HEV – annual inflation rates | 318.53 | 233.51 | 79.50 | 100.92 | 60.41 | 318.53 |
| HEV – annual risk-free returns | 287.44 | 231.51 | 74.12 | 91.07 | 56.32 | 287.44 |

Source: author's research.

The assessment of estimating balance sheet valuations of shares on the basis of the maximum and mean error is based on the assumption that the best method is the one for which the maximum and mean errors have the lowest values.

The empirical results presented in Tables 10-13 lead to the conclusion that DCF based on WIG20 is characterised by the smallest maximum error for 250 Plus companies (86.51 %). In the case of 50 Plus companies the smallest maximum error is recorded for CAPM based on WIG20 returns (276.58 %). On the other hand, HEV based on annual risk-free returns records the smallest mean error both for 250 Plus (5.06 %) and 50 Plus companies (7.84 %).

The results of the analysis indicate that in the periods of a steady increase in share values the HEV model with filtration based on the annual risk-free rate of return leads to estimations which are closest to the actual fair value in the case of assessments based on the mean error.

In the case of assessing economic and financial models on the basis of the maximum error the results closest to fair value are obtained with the use of DCF and CAPM based on WIG20 annual returns. On the other hand, the remaining indicators used in estimating balance sheet share value, including inflation rates, WIG index and average monthly increases in WIG and WIG20 indices demonstrate a lower level of correlation with balance sheet valuations of shares.

Further research of a larger number of companies in longer periods of time is likely to verify the assessment of models for estimating balance sheet valuations of shares and to test the applicability of economic and financial models.

Closing remarks. The valuation of shares and other financial instruments poses a number of problems in economic sciences, especially in accounting. These problems result from the application of the fair value category in share valuation. This concept makes a distinction between two basic types of shares: those for which prices are determined in active markets and those for which such prices and markets do not exist. The former shares are valuated on the basis of accounting principles and categories. The valuation of the latter ones is based on valuation models and techniques.

The results presented in the paper indicate that if balance sheet valuations of shares cannot rely on accounting principles and categories – especially with regard to fair value based on active market prices – valuation methods and techniques should make use of the HEV model based on risk-free rate of return (the smallest mean error) as well as CAPM based on WIG20 annual rate of return for 50 Plus and 250 Plus companies (with the smallest maximum error).

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BIELAWSKI Paweł – PhD Accounting Department Cracow University of Economics.

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